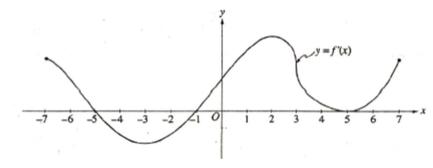
## AP PROBLEM SET #7 MAX/MIN (CURVE ANALYSIS I)

(82-6)

1. A tank with a rectangular base and rectangular sides is to be open at the top. It is to be constructed so that its width is 4 metres and its volume is 36 cubic metres. If building the tank costs \$10 per square metre for the base and \$5 per square metre for the sides, what is the cost of the least expensive tank?

(2000-3) 2.

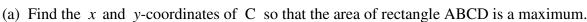


The figure above shows the graph of f', the derivative of the function f, for  $-7 \le x \le 7$ . The graph of f' has horizontal tangent lines at x = -3, x = 2, and x = 5, and a vertical tangent line at x = 3.

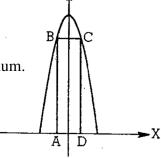
- (a) Find all values of x, for  $-7 \le x \le 7$ , at which f attains a relative minimum. Justify your answer.
- (b) Find all values of x, for  $-7 \le x \le 7$ , at which f attains a relative maximum. Justify your answer.
- (c) Find all values of x, for  $-7 \le x \le 7$ , at which  $f''(x) \le 0$ .
- (d) At what value of x, for  $-7 \le x \le 7$ , does f attain its absolute maximum? Justify your answer.

(80-2)

3. A rectangle ABCD with sides parallel to the coordinate axes is inscribed in the region enclosed by the graph of  $y = -4x^2 + 4$  and the x-axis as shown.



(b) The point C moves along the curve with its x coordinate increasing at the constant rate of 2 units per second. Find the rate of change of the area of rectangle ABCD when  $x = \frac{1}{2}$ .



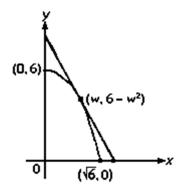
(90-5)

- 4. Let f be the function defined by  $f(x) = \sin^2 x \sin x$  for  $0 \le x \le \frac{3\pi}{2}$ .
- (a) Find the x-intercepts of the graph of f.
- (b) Find the intervals on which f is increasing.
- (c) Find the absolute maximum value and the absolute minimum value of f. Justify the answer.

- 5. Let f be the function given by  $f(x) = ln \left| \frac{x}{1+x^2} \right|$
- (a) Find the domain of f.
- (b) Determine whether f is an even function, an odd function, or neither. Justify your conclusion.
- (c) At what values of x does f have a relative maximum or a relative minimum? For each such x, use the first derivative test to determine whether f(x) is a relative maximum or a relative minimum.
- (d) Find the range of f.

(94BC-4)

6. Let  $f(x) = 6 - x^2$ . For  $0 < w < \sqrt{6}$ , let A(w) be the area of the triangle formed by the coordinate axes and the line tangent to the graph of f at the point  $(w, 6 - w^2)$ .



- (a) Find A(1)
- (b) For what value of w is A(w) a minimum?

(73-5) 7.

- (a) Find the coordinates of the absolute maximum point for the curve  $y = xe^{-kx}$  where k is a fixed positive number. Justify your answer.
- (b) Write an equation for the set of absolute maximum points for the curves  $y = xe^{-kx}$  as k varies through positive values.